



# A Level

## Mathematics

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Session: 2000 June  
Type: Mark scheme  
Code: 9200

Oxford Cambridge and RSA Examinations



**AS/A LEVEL**  
(former Cambridge linear syllabus)

A 9200  
A 9220  
AS 8473

# **MATHEMATICS/ FURTHER MATHEMATICS**

**MARK SCHEME FOR COMPONENTS**  
**TAKEN IN JUNE 2000**



INVESTOR IN PEOPLE

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## MATHEMATICS 9200

### *Component threshold marks*

Component	Maximum Mark	A	B	C	D	E	N	U
1	120	82	71	61	51	42	33	0
2	120	89	79	68	58	48	38	0
3	120	85	75	66	57	49	41	0
4	120	91	82	72	62	53	44	0

### *Overall Threshold Marks*

Option	Maximum Mark	A	B	C	D	E	N	U
A (1,2)	240	171	149	129	109	90	71	0
B (1,3)	240	164	144	125	107	89	71	0
C (1,4)	240	171	150	131	113	95	77	0

The percentage of candidates awarded each grade was as follows

Grade	A	B	C	D	E	N	U
%	36.8	16.1	13.3	12.7	8.6	7.1	5.3
Cumulative %	36.8	52.9	66.3	79.0	87.6	94.7	100.0

The total candidature was 1395



RECOGNISING ACHIEVEMENT

UCLES

Markscheme 9200/1  
June 2000

June 2000

9200/01 Linear A Level Mathematics

Question Number	Mark scheme details	Part Mark
1	Obtains ( $r =$ ) 5 OR $\sqrt{25}$ ; Obtains (centre) (0,1) AEF B1 B1	2 <u>2</u>
2	Obtains $y = 3x - 1$ Substitutes correctly into own linear equation [ $t/s^3 = 3(1/s) - 1$ ] Obtains $t = 3s^2 - s^3$ OR $t = -s^3 + 3s^2$ OR $t = s^2(3 - s)$ or other factorised form B1 M1 A1	1 2 <u>3</u>
3	(i) Obtains correct graph with numerical evidence for correct stretch s.f. $\frac{1}{2}$ B1 (ii) Obtains correct reflection in x-axis of given graph with numerical evidence B1 (iii) Obtains correct reflection of given graph in line $y = x$ with numerical evidence B1	1 1 1 <u>3</u>
4	(i) Obtains values 7,11,15 B1 (ii) Substitutes numbers in $u_n = a + (n - 1)d$ OR $u_n = a + nd$ M1 Obtains ( $u_n =$ ) $3 + 4(n - 1)$ OR $4n - 1$ AEF A1 (iii) States $v_n$ convergent AND satisfactory reason such as “ $u_n$ divergent” OR “ $v_n$ tends to zero” OR “ $u_n$ tends to infinity” B1	1 2 1 <u>4</u>
5	Method to obtain $1 \pm 6$ , with possible numerical or $x \leftrightarrow y$ errors only, seen or implied M1 Obtains $-5 < y < 7$ OR “ $-5 < y$ and $y < 7$ ” OR “ $-5 < y, y < 7$ ” CWD AEF A1 (M1 A0 for $-5 < x < 7$ etc.) Method to obtain $x \ln 2 = \ln y$ OR $x \ln 2 < \ln y$ etc. OR $x \log 2 = \log y$ M1 Obtains $\ln y$ / $\ln 2$ with no intermediate step involving $\ln(y\sqrt{2})$ (FT only on $y > 0$ ) A1✓ Obtains $x < \ln 7 / \ln 2$ ONLY having obtained positive and negative roots in first part A1	2 3 <u>5</u>

Question Number	Mark scheme details	Part Mark
6	$2 - \tan 1 = 0.4$ AND $2.4 - \tan 1.2 = -0.2$ or better	B1
	Clear identification of sign change AND deductive statement	M1
	$\{f'(x)=\} 2 - \sec^2 x$ AEF	B1
	Attempts 1.1 – $f(1.1)/f'(1.1)$	M1
	Obtains 1.18 (=1.182243....)	A1
		2
		3
		<u>5</u>
7	Valid complete attempt to find partial fractions seen or implied	M1
	Obtains $(1/2)/(x - 2) - (1/2)/(x)$ AEF	A1
	Integrates to form $A \ln(x - 2) + B \ln x$ AEF	M1
	Obtains $(1/2) \ln(x - 2) - (1/2) \ln x$ or better	A1
	Obtains $(1/2) \ln  x - 2  - (1/2) \ln  x  + c$ OR $(1/2) \ln  1 - 2/x  + c$ AEF	A1
		5
		<u>5</u>
8	(i) Sine rule used AND attempt to obtain $\sin \theta$	M1
	Obtains 0.4 OR $2/5$	A1
	(ii) $\sin^2 \theta + \cos^2 \theta = 1$ OR Pythagorean equivalent used AND attempt to obtain $\cos \theta$	M1
	Obtains $\sqrt{21}/5$ AEEF (exact working only)	A1
	(iii) Obtains $\cos BDC = 3/5$ AND $\sin BDC = 4/5$ AEEF	B1
	(iv) Indicates intention to use $\sin \theta \cos \phi \pm \cos \theta \sin \phi$	M1
	Substitution of $3/5$ ( $\checkmark$ for $\cos \phi$ ), $4/5$ ( $\checkmark$ for $\sin \phi$ ) and own $\sin \theta$ , $\cos \theta$ into attempted $\sin(\theta \pm \phi)$	M1
	Obtains $(6 + 4\sqrt{21})/25$ AEEF	A1
		2
		2
		1
		3
		<u>8</u>
9	(a) Obtains ( $A =$ ) 4	B1
	Sufficient equations for $B$ , $C$ , AND attempt to solve for $B$ OR $C$	M1
	Obtains ( $B =$ ) 5; ( $C =$ ) -1	A1 A1
	SR: only $B = 5$ or only $C = -1$ written down can score B1 for max B1 B1 M0 2/4	
	(b) Obtains $y = 2$	B1
Method to solve quadratic or cubic equation using correct formula or otherwise	M1	
Obtains $y = 4/3$ OR 1.3; $y = 8/3$ OR 2.7	A1 A1	
		4
		<u>8</u>

Question Number	Mark scheme details	Part Mark
10	<p>(i) Obtains scalar product <math>\pm 5.05</math> OR obtains three correct lengths<sup>2</sup> 25.01, 5.25, 20.16 B1  Obtains <math>\cos AOB = \pm(-3.1+4.2+0.1 \times 0.5) / \sqrt{[(-3)^2+4^2+0.1^2]} \sqrt{[1^2+2^2+0.5^2]} (=0.4407..)</math>  M1  Obtains (<math>AOB=</math>) <math>63.851^\circ</math> with 3dp required (=63.85068) A1</p> <p>(ii) Obtains (-3, 4, 0) AND (1, 2, 0) (allow position vectors or omission of 0) B1</p> <p>(iii) Obtains <math>\cos A'OB' = \pm(-3.1+4.2) / \sqrt{[(-3)^2+4^2]} \sqrt{[1^2+2^2]}</math> B1  Obtains (<math>A'OB' =</math>) <math>63^\circ</math> or better (=63.43494..) B1  Method for <math>\pm(AOB - A'OB') / A'OB'</math> M1  Obtains 0.66% AG (=0.6553... OR 0.6557...) A1</p>	3 1 4 <u>8</u>
11	<p>(i) Obtains (<math>R =</math>) 25; (<math>\alpha =</math>) <math>74^\circ</math> (= 73.73979...) B1 B1  Attempt to use inverse sine to find one value of <math>(\theta + \alpha)</math> for <math>\sin(\theta + \alpha) = -3/R</math> M1  Obtains any <math>\theta</math> satisfying <math>\sin(\theta + \alpha) = -3/R</math> for own values of <math>R</math> and <math>\alpha</math> A1✓  Obtains (<math>\theta =</math>) <math>-81^\circ</math>; <math>113^\circ</math> (= -80.631...) (= 113.1523...) A1 A1  SR: -A1 mark for all extra solutions in range</p> <p>(ii) (a) Method to add <math>10^\circ</math> to previous solution(s) M1  Obtains (<math>x =</math>) <math>\theta^\circ + 10</math> within range specified (= <math>123^\circ = 123.1523...</math>) A1✓</p> <p>(b) Method for <math>90 - y = \theta</math> M1  Obtains (<math>y =</math>) <math>90 - \theta^\circ</math> within range specified (= <math>171^\circ = 170.639...</math>) A1✓  SR: Fresh starts for (a) and (b) earn M1 for full correct method, A1 correct answer</p>	2 4 2 2 <u>10</u>
12	<p>Uses <math>dx = \pm \cos \theta (d\theta)</math> correctly M1  Obtains <math>\pm \sin^2 \theta \cos^2 \theta</math> correctly M1  Change of limits and use of double angle formula to obtain given integral AG A1</p> <p>Obtains <math>\int a + b \cos 4\theta (d\theta)</math> M1</p> <p>Obtains <math>\frac{1}{8} \left( \theta - \frac{1}{4} \sin 4\theta \right)</math> AEF A1</p> <p>Obtains (<math>A =</math>) <math>\frac{1}{8} \left( \frac{\pi}{6} - \frac{\sqrt{3}}{8} \right)</math> AEEF (=0.038386) A1</p> <p>Use of <math>\int y^2 dx</math> where <math>y = x^2 \sqrt{1-x^2}</math> M1</p> <p><math>\pi \int x^4 (1-x^2) (dx)</math> seen A1</p> <p>Attempts to evaluate <math>[ax^5 + bx^7]_0^{\frac{1}{2}}</math> M1</p> <p>Obtains (<math>V =</math>) <math>23\pi/4480</math> AEEF A1</p>	3 3 4 <u>10</u>



Question Number	Mark scheme details	Part Mark	
13	(i) Obtains $y - 6 = m(x + 1)$ for some $m$	M1	3
	Obtains $m = -2$	B1	
	Obtains $\pm(2x + y - 4) = 0$	A1	
	(ii) Complete method to solve equations $l$ and $l'$ simultaneously	M1	2
	Obtains $x = 3$ AND $y = -2$	A1	
	(iii) Complete method for magnitude of displacement from $P$ to intersection (ii)	M1	2
	Obtains correctly $4\sqrt{5}$ AG ( $=\sqrt{4^2 + 8^2}$ )	A1	
	(iv) Obtains $(QR =) \sqrt{320}$ AEEF	B1	3
	Any complete method for area of triangle PQR	M1	
	Obtains 80 by an exact method	A1	
	<b>OR</b> Any complete exact method for area of triangle	M1	3
	Obtains $A = 16 \times 13 - 3 \times 13 - 5 \times 5 - 8 \times 8$ AEEF	A1	
	or $A = \frac{1}{2}((-1 \times -7) + (-7 \times 1) + (9 \times 6) - (6 \times -7) - (-7 \times 9) - (1 \times -1))$ AEEF	A1	
Obtains 80 by an exact method	A1		
		<b>10</b>	
14	$dm/dt = ; -km$ OR $km$ with $k < 0$ stated AEF	B1 B1	2
	NB: Allow B1 B0 if finds $dm/dt$ from AG		
	Separation of variables and attempt to integrate	M1	4
	Obtains $\ln m = \pm kt + c$ consistent with first part	A1	
	Obtains $c = \pm \ln m_0$ or equivalent and attempts to substitute and exponentiate correctly	M1	
	Obtains correctly $m = m_0 e^{-kt}$ AG	A1	4
	<b>OR</b> Uses $dm/dt \pm km = 0$ and find integrating factor $e^{\pm kt}$	M1	
	Obtains $m e^{\pm kt} = c$	A1	
	Obtains $c = m_0$ and rearranges	M1	
	Obtains correctly $m = m_0 e^{-kt}$ AG	A1	4
	<b>SR:</b> Obtains $m = e^{-kt}$ can score B1 B1 M1 B1 max. 4/6		
	(i) Graph with positive gradient and gradient decreasing	B1	2
	Graph passes through $M(0) > 0$ and limiting from below (ignore all labels)	B1	
(ii) States that $M$ tends to $A$	B1	1	
(iii) Uses $dM/dt = -dm/dt$ or equivalent	M1	2	
Complete correct substitution to obtain given differential equation AG	A1		
		<b>11</b>	

Question Number	Mark scheme details	Part Mark
15	<p>Uses <math>r^2\theta/2</math> and two radii M1</p> <p>Obtains (<math>A =</math>) <math>14\theta</math> (cm<sup>2</sup>) A1</p> <p>(i) Attempts to differentiate own <math>A</math> with respect to <math>t</math> and use 0.1 M1</p> <p>Obtains <math>1.4</math> (cm<sup>2</sup>s<sup>-1</sup>) CWD A1</p> <p>(ii) (<math>P =</math>) <math>2+2+8\theta+6\theta</math> OR <math>4 + 14\theta</math> OR <math>NP + MQ = 14\theta</math> and <math>MN, PQ</math> constant M1</p> <p>Obtains <math>1.4</math> (cm s<sup>-1</sup>) from correct <math>P</math> CWD A1</p> <p>(iii) Uses completely correct cosine rule in triangle including <math>\theta</math> and <math>L</math> M1</p> <p>Obtains <math>L^2 = 100 - 96\cos\theta</math> AG A1</p> <p>Uses <math>\frac{dL}{dt} = \frac{dL}{d\theta} \frac{d\theta}{dt}</math> M1</p> <p>Obtains <math>2L</math> in denominator or <math>\frac{1}{2}(100 - 96\cos\theta)^{-\frac{1}{2}}</math> B1</p> <p>Obtains <math>96\sin\theta d\theta/dt</math> OR <math>96\sin\theta(0.1)</math> AEF B1</p> <p>Substituting for <math>\theta, d\theta/dt</math> M1</p> <p>Obtains <math>(6\sqrt{39})/65</math> OR <math>0.58</math> (<math>= 0.57646\dots</math>) (cm s<sup>-1</sup>) A1</p>	<p>2</p> <p>2</p> <p>2</p> <p>2</p> <p>2</p> <p>5</p> <p><b>13</b></p>
16	<p>(i) (a) Obtains <math>4p + 16q = 1</math> B1</p> <p>(<math>dy/dx =</math>) <math>2px + 4qx^3</math> B1</p> <p>Substitutes to obtain <math>\sqrt{2}(a(4p + 16q))</math> B1</p> <p>Demonstrates using <math>4p + 16q = 1</math> that <math>2p(\sqrt{2}) + 4q(\sqrt{2})^3 = \sqrt{2}/2</math> AG B1</p> <p>(b) Obtains <math>a = 5/36</math> OR <math>0.14</math> (<math>= 0.13888\dots</math>) B1</p> <p>Obtains first term <math>ax^2</math> ✓ (<math>= 5x^2/36 = 0.14x^2</math>) B1✓</p> <p>Obtains second non zero term <math>ax^4/9</math> ✓ (<math>= 5x^4/324 = 0.015x^4</math>) B1✓</p> <p>(c) Obtains <math>k = 0.181</math> (<math>= 0.181015\dots</math>) B1</p> <p>Attempt to substitute up to <math>x^4</math> term for <math>e^x</math> AND, using <math>-x</math>, for <math>e^{-x}</math> M1</p> <p>Obtains <math>kx^2 + kx^4/12 + \dots</math> or better (<math>= 0.181x^2 + 0.0151x^4</math>) A1</p> <p>(ii) Show clearly that 40 comes from <math>2 \times 20</math> (where 20 can be assumed) B1</p> <p>Expands series with <math>e^x</math> and states <math>x = 0.1r</math></p> <p><b>OR</b> Shows sum of individual terms at start (before seeing summation sign) B1</p> <p>ie see <math>e^{0.1} + e^{0.2} + \dots + e^{-0.1} + e^{-0.2} + \dots</math></p> <p>Identifies a G.P. and its common ratio correctly M1</p> <p>Attempts valid method for both summations with '<math>r</math>' = <math>e^{0.1}</math> AND <math>e^{-0.1}</math> M1</p> <p>Obtains (sum =) <math>6.4</math> (<math>= 6.40\dots</math>) A1</p>	<p>1</p> <p>3</p> <p>1</p> <p>2</p> <p>1</p> <p>2</p> <p>2</p> <p>2</p> <p>3</p> <p><b>15</b></p>



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RECOGNISING ACHIEVEMENT

UCLES

Markscheme 9200/2  
June 2000

June 2000

9200/02 A Level Linear Mathematics

1	<p>EITHER: Attempt quotient rule (or equivalent) allowing sign errors for this mark (products reversed only)</p> <p>Obtain any correct unsimplified expression, e.g. <math>\frac{(2x+1) \times 1 - (x-2) \times 2}{(2x+1)^2}</math></p> <p>Obtain simplified answer <math>\frac{5}{(2x+1)^2}</math> correctly</p> <p>[Product rule also requires chain rule (both applied correctly for M1)]</p> <p>OR: Express the function as <math>\frac{1}{2} - \frac{5}{2(2x+1)}</math></p> <p>Use chain rule to differentiate <math>k(2x+1)^{-1}</math> (result <math>-k(2x+1)^{-2}</math> is M0)</p> <p>Obtain simplified answer <math>\frac{5}{(2x+1)^2}</math> correctly</p> <p>[Accept final answer in the form <math>\frac{5}{4x^2+4x+1}</math>.]</p>	<p>M1 A1 A1 B1 M1 A1</p>	3
2	<p>EITHER: State or imply correct cosine rule (in any form) involving 2, 3, 4 and either <math>B</math> or <math>C</math></p> <p>Obtain <math>\cos B = -\frac{1}{4}</math> (aef) or <math>B = 104.5^\circ</math> or <math>104^\circ</math> or <math>105^\circ</math> or <math>\cos C = \frac{7}{8}</math> (aef) or <math>C = 29^\circ</math></p> <p>State or imply correct formula for <math>AD^2</math> involving 2, 4 and their numerical <math>\cos B</math> or 1, 4 and their numerical <math>\cos(180 - C)</math> or <math>-\cos C</math></p> <p>Obtain answer <math>\sqrt{24}</math> or <math>2\sqrt{6}</math> or 4.9</p> <p>OR: [E is the foot of the perpendicular from A to CB produced]</p> <p>Use Pythagoras in triangles ACE and ABE to obtain an equation for BE or AE</p> <p>Obtain <math>BE = \frac{1}{2}</math> or <math>AE^2 = \frac{15}{4}</math></p> <p>Apply Pythagoras (or trig) with numerical BE and/or AE to find <math>AD^2</math> (or AD)</p> <p>Obtain answer <math>\sqrt{24}</math> or <math>2\sqrt{6}</math> or 4.9</p>	<p>M1* A1 M1 (dep *) A1 M1* A1 M1 (dep *) A1</p>	4
3	<p>(i) Multiply two relevant probabilities for a 'Yes' branch</p> <p>Add the two relevant two-factor cases, i.e. <math>\frac{2}{3}p + \frac{1}{3}(1-p)</math></p> <p>Obtain given answer <math>\frac{1}{3}(1+p)</math> correctly</p> <p>(ii) (Solve <math>\frac{1}{3}(1+p)</math> and) find <math>p = 0.05</math></p> <p>Divide attempted P('No' and 'Truthful') by P('No')</p> <p>State or imply answer is <math>\frac{\frac{2}{3}(1-0.05)}{1-0.35}</math></p> <p>Obtain answer 0.97 or <math>\frac{38}{39}</math> or equivalent fraction</p> <p>[M1 is for a fraction with numerical numerator <math>\frac{2}{3}(1-p)</math> or denominator <math>1-0.35</math> (or equivalent); ft only if <math>0 &lt; p &lt; 1</math>]</p>	<p>M1* M1 (dep *) A1 B1 M1 A1 ft A1</p>	3 1 3

4	(a) (i) State 'pie chart' or 'bar chart' or 'pictogram' or 'line diagram'	B1	1
	(ii) State 'histogram' or 'stem and leaf diagram' or 'frequency polygon' or 'cumulative frequency diagram'	B1	1
	(iii) State 'double bar chart' or 'two bar charts with common scales on a single diagram'	B1	1
(b) (i) Read off at least one relevant result Obtain any one answer 32, 38, 43 Obtain all three correct values of the median and quartiles, identifying the median State interquartile range is 11	M1	4	
	A1		
	A1 ft		
(ii) Show linear scale from 0 to 60 with 0 and 60 marked and with ends of whiskers located at 5 and 60 Show box extending between their quartile values Show median line in box at their median value [Location of 5, medians and quartiles to be reasonably consistent with a linear scale.]	B1 B1 ft B1 ft	3	
5	EITHER: Use the connected formula $s = ut + \frac{1}{2}at^2$  Obtain equation $6 = 15t - \frac{1}{2}gt^2$  Solve a quadratic equation for $t$ Obtain roots 0.47 and 2.6  OR: Use the correct formula $v^2 = u^2 + 2as$ to find $v$  State correct expression $\sqrt{(15^2 - 2g \times 6)}$ for speed at height 6m  Use a correct formula to evaluate a relevant time Obtain answers 0.47 and 2.6 [Treat 'time above 6m' as a MR and give maximum possible on scheme.]	M1 * A1 M1 (dep *) A1 M1 * A1 M1 (dep *) A1	4
6	(i) Show three corrected line segments with 2 correctly signed gradients Show or imply $t$ and $v$ axes with relevant points (10, 40), (15, 30) and (20, 0) identified and graph of correct shape Carry out complete method for the area calculation, e.g. two triangles and one trapezium (or equivalent use of constant acceleration formulas) Obtain answer 450	B1 B1 M1 A1	4
	(ii) Sketch a graph starting at $O$ having positive, decreasing gradient	B1	1
7	Equate total momentum before and after State or imply a correct equation $20000 \times 1.5 + 10000 \times 1 = (20000 + 10000)v$ Obtain answer $\frac{4}{3}$ , or equivalent, correctly	M1 A1 A1	3
	(i) State either $5000 = (\pm)30000a$ or both of $5000 - P = (\pm)10000a$ and $P = (\pm)20000a$  Obtain answer $(\pm)\frac{1}{6}$ , or equivalent, for the deceleration	M1 A1	2
	(ii) Use a Newton II equation for one of the trucks with their numerical $a$ (or numerical $v$ and $t$ ) to find $P$ Obtain answer $(\pm)3333\frac{1}{3}$ or 3300 only  [if $g$ appears in the momentum equation deduct A1 but allow A1 for answer $\frac{4}{3}$ or equivalent.]	M1 A1	2



10	<p>(a) (i) State any one Newton II equation, e.g. <math>0.3g - T = 0.3a</math>, <math>T - 0.2g = 0.2a</math>, <math>0.1g = 0.5a</math>            State two of the above equations correctly            Solve a relevant pair of equations to find <math>T</math>            Obtain answer <math>T = 2.4</math></p> <p>(ii) State or use <math>a = \frac{1}{5}g</math> in this part of the question            Use <math>v = u + at</math> with <math>u = 0</math> and <math>a \neq g</math> to find <math>t</math>            Obtain answer <math>t = 2.0</math></p> <p>[Answers to (i) and (ii) left as <math>6g/25</math> and <math>20/g</math> are penalised once, scoring A0 A1]            [NB: if <math>g</math> is omitted only the M marks are available.]</p> <p>(b) EITHER: State equation or inequality, with 3 force terms, for motion parallel to the plane for either particle            Resolve perpendicular to the plane for either particle, and use <math>F = \mu R</math>            State one correct equation/inequality, e.g.  <math>0.3g \sin 30^\circ - 0.3\mu g \cos 30^\circ - T = 0.3a</math> (or <math>&gt; 0</math> or <math>= 0</math>)            State a second correct equation/inequality, e.g.  <math>T - 0.2g \sin 30^\circ - 0.2\mu g \cos 30^\circ = 0.2a</math> (or <math>&gt; 0</math> or <math>= 0</math>)            Eliminate <math>T</math> from a pair of equations or inequalities and solve for <math>\mu</math>            Obtain the given inequality <math>\mu &lt; \frac{1}{5\sqrt{3}}</math> correctly and not via decimals</p> <p>OR: State 'system' equation or inequality involving both weight components and both friction forces            Resolve perpendicular to the plane for both particles, and use <math>F = \mu R</math>            State any correct equation/inequality, e.g. <math>0.1g \sin 30^\circ - 0.5\mu g \cos 30^\circ = 0.5a</math> (or <math>&gt; 0</math> or <math>= 0</math>)            Solve this equation/inequality for <math>\mu</math>            Obtain given inequality <math>\mu &lt; \frac{1}{5\sqrt{3}}</math> correctly and not via decimals</p>	<p>M1 A1 M1 A1 B1 M1 A1 M1 M1 A1 M1 M1 A1 M1 M1 A2 M1 A1</p>	<p>4 3 6</p>
11	<p>State procedure A is better            Indicate that early customers may not be typical of customers in general            [for the justification mark, it's no good <i>merely</i> saying 'not random' or 'biased'.]            State any sensible idea, involving e.g. useful criticisms from people who don't use her shop, useful ideas for attracting new customers, etc, etc.            [For this mark it is not enough <i>merely</i> saying 'to be more random' or 'to avoid bias']</p>	<p>B1 B1 B1</p>	<p>2 1</p>
12	<p>Form an expression for <math>\Sigma x^2 p</math>            Subtract <math>(\Sigma xp)^2</math> from the above            Obtain correct expression <math>6p - 16p^2</math> for the variance            Equate variance (not s.d.) to <math>\frac{1}{2}</math> and solve for <math>p</math>            Obtain values <math>p = \frac{1}{4}</math> and <math>p = \frac{1}{8}</math>            Deduce both values 1 and <math>\frac{1}{2}</math> for <math>E(X)</math>            [The ft is only on 2 <math>p</math> values with <math>0 &lt; p &lt; 1</math>]</p>	<p>M1* M1 (dep*) A1 M1 A1 A1 ft</p>	<p>6</p>
13	<p>(i) State or imply one of the two binomial terms, <math>\binom{50}{1}(0.88)^{49}(0.12)</math> and  <math>\binom{50}{2}(0.88)^{48}(0.12)^2</math>            Add the correct three binomial terms (and no others)            Obtain answer 0.051</p> <p>(ii) State or imply <math>\mu = 50 \times 0.12</math>            State or imply value <math>50 \times 0.12 \times 0.88</math> relating to variance/s.d.            Evaluate <math>\frac{9.5-6}{\sqrt{5.28}}</math> and use tables            Obtain answer 0.064            [The M1 is not lost for missing continuity correction, or for cc of on the wrong side, but the denominator must be <math>\sqrt{npq}</math> not <math>npq</math>.]            [Use of exact binomial terms scores M0; incorrect use of Poisson approximation can score B1 for <math>\mu = 6</math> and is allowed B1 for final answer 0.084.]            [Treat the use of <math>p = \frac{12}{50}</math> as a MR.]            [If <math>p, q</math> interchanged, all M marks and a B1 are available.]</p>	<p>M1 M1 A1 B1 B1 M1 A1</p>	<p>3 4</p>

14	<p>(i) State value 8900 for <math>\hat{\mu}</math></p> <p>State or imply expression <math>\frac{1}{74} \left( 5.978 \times 10^9 - \frac{(6.675 \times 10^5)^2}{75} \right)</math>, or equivalent</p> <p>Obtain answer 503000 for <math>\hat{\sigma}^2</math></p> <p>[If done by calculator with no working shown, the mark for the variance estimate is effectively B2 or B0. The biased estimate gets 0/2]</p> <p>(ii) Use of <math>\hat{\mu} \pm z \times \sqrt{\left(\frac{\hat{\sigma}^2}{75}\right)}</math>, with numerical values throughout</p> <p>Use of correct z-value, i.e. 1.96</p> <p>Obtain correct interval correctly <math>8740 &lt; \mu &lt; 9060</math> (allow <math>8900 \pm 160</math>)</p> <p>[The M mark can also be earned for <math>\sqrt{\left(\frac{s^2}{74}\right)}</math>, where <math>s^2</math> is the biased variance estimate; for this mark, z must be numerical tabular value. However the use of <math>\sqrt{\left(\frac{s^2}{75}\right)}</math> can only earn M1 B1 A0.]</p> <p>State or use the correct z-value <math>-1.28(2)</math></p> <p>Form an equation <math>\frac{a-8900}{\sqrt{(503000)}} = z</math>, where z is a tabular value (ignore a sign error in z here)</p> <p>Obtain answer 7990</p>	<p>B1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>B1</p> <p>A1</p> <p>B1</p> <p>M1</p> <p>A1</p>	<p></p> <p></p> <p>3</p> <p></p> <p></p> <p></p> <p></p> <p></p> <p></p> <p></p> <p>3</p>
15	<p>Show evidence of substituting relevant numbers into a correct formula</p> <p>Obtain answer 0.99 correctly</p> <p>[If done by calculator with no working, the marks are B3 or B0]</p> <p>Make a sensible comment, e.g. consistent with a linear relationship, strong positive correlation</p> <p>Use the <math>d-v</math> data correctly to find the line of <math>d</math> on <math>v</math></p> <p>Obtain equation <math>d = -25.5 + 1.64v</math></p> <p>[If done by calculator with no working, the marks are B2 or B0]</p> <p>Show axes with required scaling</p> <p>Show the six points plotted correctly</p> <p>Show the calculated line correctly</p> <p>[For the final B mark check that the <math>v</math>-intercept and ordinate at <math>v = 40</math> are accurate to <math>\pm \frac{1}{2}</math> square, or make a similar check]</p> <p>Use the equation or plot of the regression line and obtain <math>d = 65</math> or <math>64</math> completely correctly</p> <p>Make any sensible comment, e.g. plot of data shows evidence of a non-linear relationship. Regression line overestimates <math>d</math> when <math>v = 55</math> OR value of coefficient (or data plot) suggests use of line will be suitable</p>	<p>M1</p> <p>A2</p> <p>B1</p> <p>M1</p> <p>A1</p> <p>B1</p> <p>B1</p> <p>B1 ft</p> <p>B1</p> <p>B1</p>	<p></p> <p>3</p> <p>1</p> <p>2</p> <p></p> <p>3</p> <p>1</p> <p>1</p>



16	(i) State numerical expression of the form $\left(\frac{3}{4}\right)^n \left(\frac{1}{4}\right)$ with $n = 3$ or 4	M1	2
	Obtain answer $\frac{27}{256}$ Or 0.11	A1	
	(ii) EITHER: Attempt addition of relevant terms $\left(\frac{3}{4}\right)^n \left(\frac{1}{4}\right)$	M1	2
	Obtain answer $\frac{21087}{65536}$ or 0.32	A1	
	OR: Attempt relevant subtraction $\left(\frac{3}{4}\right)^3 - \left(\frac{3}{4}\right)^8$	M1	2
	Obtain answer $\frac{21087}{65536}$ or 0.32	A1	
	(iii) State expression $\left(\frac{3}{4}\right)\left(\frac{1}{4}\right)^2$ for one case	B1	3
	Add probabilities for the two cases FSS, SFS (or equivalent)	M1	
	Obtain answer $\frac{3}{32}$ or 0.094	A1	
	State or imply value 4 for mean $\mu$ of $X$	B1	5
State or imply value 12 for variance $\sigma^2$ of $X$	B1		
Show numerical calculation $\frac{5-\mu}{\text{st. error}}$ where the attempted denominator involves both their 12 and 60	M1		
Show correct expression $\frac{5-4}{\sqrt{\left(\frac{12}{60}\right)}}$	A1 ft		
Obtain answer 0.013 correctly	A1		



RECOGNISING ACHIEVEMENT

UCLES

Markscheme 9200/3  
June 2000

June 2000

9200/03 A Level Linear Mathematics

1	<p>EITHER: Attempt quotient rule (or equivalent) allowing sign errors for this mark (products reversed only)</p> <p>Obtain any correct unsimplified expression, e.g. <math>\frac{(2x+1) \times 1 - (x-2) \times 2}{(2x+1)^2}</math></p> <p>Obtain simplified answer <math>\frac{5}{(2x+1)^2}</math> correctly</p> <p>[Product rule also requires chain rule (both applied correctly for M1)]</p> <p>OR: Express the function as <math>\frac{1}{2} - \frac{5}{2(2x+1)}</math></p> <p>Use chain rule to differentiate <math>k(2x+1)^{-1}</math> (result <math>-k(2x+1)^{-2}</math> is M0)</p> <p>Obtain simplified answer <math>\frac{5}{(2x+1)^2}</math> correctly</p> <p>[Accept final answer in the form <math>\frac{5}{4x^2+4x+1}</math>.]</p>	<p>M1</p> <p>A1</p> <p>A1</p> <p>B1</p> <p>M1</p> <p>A1</p>	3
2	<p>EITHER: State or imply correct cosine rule (in any form) involving 2, 3, 4 and either B or C</p> <p>Obtain <math>\cos B = -\frac{1}{4}</math> (aef) or <math>B = 104.5^\circ</math> or <math>104^\circ</math> or <math>105^\circ</math> or <math>\cos C = \frac{7}{8}</math> (aef) or <math>C = 29^\circ</math></p> <p>State or imply correct formula for <math>AD^2</math> involving 2, 4 and their numerical <math>\cos B</math> or 1, 4 and their numerical <math>\cos(180 - C)</math> or <math>-\cos C</math></p> <p>Obtain answer <math>\sqrt{24}</math> or <math>2\sqrt{6}</math> or 4.9</p> <p>OR: [E is the foot of the perpendicular from A to CB produced]</p> <p>Use Pythagoras in triangles ACE and ABE to obtain an equation for BE or AE</p> <p>Obtain <math>BE = \frac{1}{2}</math> or <math>AE^2 = \frac{15}{4}</math></p> <p>Apply Pythagoras (or trig) with numerical BE and/or AE to find <math>AD^2</math> (or AD)</p> <p>Obtain answer <math>\sqrt{24}</math> or <math>2\sqrt{6}</math> or 4.9</p>	<p>M1*</p> <p>A1</p> <p>M1 (dep *)</p> <p>A1</p> <p>M1*</p> <p>A1</p> <p>M1 (dep *)</p> <p>A1</p>	4
3	<p>(i) Multiply two relevant probabilities for a 'Yes' branch</p> <p>Add the two relevant two-factor cases, i.e. <math>\frac{2}{3}p + \frac{1}{3}(1-p)</math></p> <p>Obtain given answer <math>\frac{1}{3}(1+p)</math> correctly</p> <p>(ii) (Solve <math>\frac{1}{3}(1+p)</math> and) find <math>p = 0.05</math></p> <p>Divide attempted P('No' and 'Truthful') by P('No')</p> <p>State or imply answer is <math>\frac{\frac{2}{3}(1-0.05)}{1-0.35}</math></p> <p>Obtain answer 0.97 or <math>\frac{38}{39}</math> or equivalent fraction</p> <p>[M1 is for a fraction with numerical numerator <math>(1-p)</math> or denominator <math>1-0.35</math> (or equivalent); ft only if <math>0 &lt; p &lt; 1</math>]</p>	<p>M1*</p> <p>M1 (dep *)</p> <p>A1</p> <p>B1</p> <p>M1</p> <p>A1 ft</p> <p>A1</p>	<p>3</p> <p>1</p> <p>3</p>

4	<p>(a) (i) State 'pie chart' or 'bar chart' or 'pictogram' or 'line diagram'</p> <p>(ii) State 'histogram' or 'stem and leaf diagram' or 'frequency polygon' or 'cumulative diagram'</p> <p>(iii) State 'double bar chart' or 'two bar charts with common scales on a single diagram'</p> <p>(b) (i) Read off at least one relevant result Obtain any one answer 32, 38, 43 Obtain all three correct values of the median and quartiles, identifying the median State interquartile range is 11</p> <p>(ii) Show linear scale from 0 to 60 with 0 and 60 marked with ends of whiskers located at 5 and 60 Show box extending between their quartile values Show median line in box at their median value</p> <p>[Location of 5, medians and quartiles to be reasonably consistent with a linear scale.]</p>	<p>B1</p> <p>B1</p> <p>B1</p> <p>M1</p> <p>A1</p> <p>A1</p> <p>A1 ft</p> <p>B1</p> <p>B1 ft</p> <p>B1 ft</p>	<p>1</p> <p>1</p> <p>1</p> <p>4</p> <p>3</p>
5	<p>EITHER: Use the correct formula <math>s = ut + \frac{1}{2}at^2</math></p> <p>Obtain equation <math>6 = 15t - \frac{1}{2}gt^2</math></p> <p>Solve a quadratic equation for <math>t</math></p> <p>Obtain roots 0.47 and 2.6</p> <p>OR: Use the correct formula <math>v^2 = u^2 + 2as</math> to find <math>v</math></p> <p>State correct expression <math>\sqrt{(15^2 - 2g \times 6)}</math> for speed at height 6m</p> <p>Use a correct formula to evaluate a relevant time</p> <p>Obtain answers 0.47 and 2.6</p> <p>[Treat 'time above 6m' as a MR and give maximum possible on scheme.]</p>	<p>M1 *</p> <p>A1</p> <p>M1 (dep *)</p> <p>A1</p> <p>M1 *</p> <p>A1</p> <p>M1 (dep *)</p> <p>A1</p>	<p>4</p>
6	<p>(i) Show three corrected line segments with 2 correctly signed gradients Show or imply <math>t</math> and <math>v</math> axes with relevant points (10, 40), (15, 30) and (20, 0) identified and graph of correct shape Carry out complete method for the area calculation, e.g. two triangles and one trapezium (or equivalent use of constant acceleration formulas) Obtain answer 450</p> <p>(ii) Sketch a graph starting at <math>O</math> having positive, decreasing gradient</p>	<p>B1</p> <p>B1</p> <p>M1</p> <p>A1</p> <p>B1</p>	<p>4</p> <p>1</p>
7	<p>(i) State moments equation about <math>A</math>: <math>F \times 2\sin BAC = W \times \frac{1}{2}AC</math>, or equivalent</p> <p>State or imply any correct trig result, e.g. <math>\tan BAC = \frac{1}{2}</math>, or perp distance from <math>B</math> to <math>AC = \frac{2}{\sqrt{5}}</math>, or equivalent</p> <p>Obtain answer <math>F = \frac{5}{4}W</math> correctly</p> <p>(ii) Obtain <math>\tan \theta = \frac{W}{\frac{5}{4}W}</math> (or <math>= \frac{\text{perp distance from } B \text{ to } AC}{\frac{1}{2}AC}</math>)</p> <p>Obtain <math>R = \sqrt{\left(\frac{25}{16}W^2 + W^2\right)}</math> (or from <math>R = \frac{F}{\cos \theta}</math>)</p> <p>Obtain <math>R \frac{W\sqrt{41}}{4} (= 1.6W)</math> AND <math>\theta = 39^\circ</math> (with <math>R</math> clearly in the correct direction)</p>	<p>M1</p> <p>B1</p> <p>A1</p> <p>B1 ft</p> <p>B1 ft</p> <p>B1</p>	<p>3</p>
8	<p>Equate total momentum before and after</p> <p>State or imply a correct equation <math>20000 \times 1.5 + 10000 \times 1 = (20000 + 10000)v</math></p> <p>Obtain answer <math>\frac{4}{3}</math>, or equivalent, correctly</p> <p>(i) State either <math>5000 = (\pm)30000a</math> or both of <math>5000 - P = (\pm)10000a</math> and <math>P = (\pm)20000a</math></p> <p>Obtain answer <math>(\pm)\frac{1}{6}</math>, or equivalent, for the deceleration</p> <p>(ii) Use a Newton II equation for one of the trucks with their numerical <math>a</math> (or numerical <math>v</math> and <math>t</math>) to find <math>P</math></p> <p>Obtain answer <math>(\pm)3333\frac{1}{3}</math> or 3300 only</p> <p>[if <math>g</math> appears in the momentum equation deduct A1 but allow A1 for answer or equivalent.]</p>	<p>M1</p> <p>A1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p>	<p>3</p> <p>2</p> <p>2</p>

9	<p>Use Hooke's law in equilibrium equation <math>0.5g = \frac{1.2\lambda}{0.6}</math></p> <p>Obtain <math>\lambda = \frac{1}{4}g</math> or 2.5(2.4525)</p> <p>State energy equation involving KE and at least one of EE, PE</p> <p>Show correct PE term <math>0.5 \times g \times 1.8</math></p> <p>Show correct EE term <math>\frac{\frac{1}{4}g \times 1.2^2}{2 \times 0.6}</math> (= 0.3g)</p> <p>State unsimplified equation, e.g. <math>0.25v^2 + 0.3g = 0.9g</math> (signs correct)</p> <p>Obtain answer <math>v = 4.8</math> or 4.9 correctly</p> <p>[For the B marks for the PE and EE terms, ignore signs.]</p>	<p>M1</p> <p>A1</p> <p>M1</p> <p>B1</p> <p>B1 ft</p> <p>A1 ft</p> <p>A1</p>	<p>2</p> <p>5</p>
10	<p>Resolve vertically, i.e. <math>2T\cos\theta = W</math> or use trig in correct triangle or use Lami</p> <p>Obtain answer <math>41^\circ</math> following correct use of <math>T = \frac{2}{3}W</math></p> <p>EITHER: Attempt a resolving equation, with 3 terms</p> <p>Obtain a correct equation in <math>T</math> and trig ratios of one angle, e.g. one of <math>T\cos\theta + T\sin\theta = W</math>, <math>T\cos\theta - T\sin\theta = \frac{1}{2}W</math>, <math>T = \frac{1}{2}W\cos\theta + W\sin\theta</math>, <math>T = W\cos\theta - \frac{1}{2}W\sin\theta</math> (allow <math>\cos(90 - \theta)</math> for <math>\sin\theta</math> etc)</p> <p>Attempt a second independent 3-term resolving equation</p> <p>Obtain a second correct equation in <math>T</math> and trig ratios of previous angle</p> <p>Obtain an equation in <math>\theta</math> (or <math>T</math>) only</p> <p>Obtain angle <math>18^\circ</math> or <math>72^\circ</math></p> <p>Obtain <math>T = 0.79W</math> or equivalent</p> <p>OR:</p> <p>State resultant of <math>W</math> forces has magnitude <math>\frac{\sqrt{5}}{2}W</math> or equivalent</p> <p>Combine <math>T</math> forces and equate resultants</p> <p>Obtain a correct equation, e.g. <math>2T\cos45^\circ = \frac{\sqrt{5}}{2}W</math></p> <p>Obtain <math>T = 0.79W</math> or equivalent</p> <p>State resultant of <math>W</math> forces makes <math>\tan^{-1}\left(\frac{1}{2}\right)</math> with the vertical or <math>\tan^{-1}(2)</math> with the horizontal</p> <p>Equate directions and obtain an equation in <math>\theta</math>, using <math>45^\circ</math> or <math>135^\circ</math></p> <p>Obtain angle <math>18^\circ</math> or <math>72^\circ</math></p> <p>[SR: Use of <math>Wg</math> for the weight <math>W</math> can score M1 A0 then M3 and as A1.]</p>	<p>M1</p> <p>A1</p> <p>M1*</p> <p>A1</p> <p>M1*</p> <p>A1</p> <p>M1 (dep *)</p> <p>A1</p> <p>A1</p> <p>B1</p> <p>M1</p> <p>A1</p> <p>A1</p> <p>B1</p> <p>M1</p> <p>A1</p>	<p>2</p> <p>7</p>
11	<p>EITHER: State a correct equation from which <math>T</math> or <math>\frac{1}{2}T</math> can be found,</p> <p>e.g. <math>0 = V\sin\theta - \frac{1}{2}gt^2</math> or <math>0 = V\sin\theta - gt</math></p> <p>Obtain any correct expression for <math>R</math> in terms of <math>V</math>, <math>\theta</math> and <math>g</math></p> <p>Obtain given answer <math>R = \frac{V^2\sin2\theta}{g}</math> correctly</p> <p>OR:</p> <p>Using the equation of trajectory, state or imply equation</p> <p><math>0 = R\tan\theta - \frac{gR^2}{2V^2\cos^2\theta}</math>, or equivalent</p> <p>Obtain any correct expression for <math>R</math> in terms of <math>V</math>, <math>\theta</math> and <math>g</math></p> <p>Obtain given answer <math>R = \frac{V^2\sin2\theta}{g}</math> correctly</p> <p>State any one suitable assumption, e.g. no air resistance, constant acceleration, etc</p> <p>(i) State both <math>D - 100 = \frac{U^2\sin60^\circ}{g}</math> and <math>D + 100 = \frac{U^2\sin90^\circ}{g}</math> or equivalent</p> <p>Eliminate <math>D</math> and solve for <math>U^2</math></p> <p>Obtain given answer 121 correctly</p> <p>(ii) Obtain <math>D = 1400</math> (1392.82)</p> <p>Substitute values of <math>U</math> and <math>D</math> in range equation and solve for <math>\sin2\theta</math></p> <p>Obtain answer <math>34^\circ</math> (34.4547...) or <math>35^\circ</math></p> <p>[SR: use of GA to show <math>U = 121</math> and <math>D = 1400</math> are consistent can get B1 M0 A0 B1 M1 A1.]</p>	<p>M1</p> <p>A1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>A1</p> <p>B1</p> <p>B1</p> <p>M1</p> <p>A1</p> <p>B1</p> <p>M1</p> <p>A1</p>	<p>3</p> <p>1</p> <p>3</p> <p>3</p>

12	<p>EITHER: State <math>mg = T\cos\alpha</math>            Equate <math>T\sin\alpha</math> to <math>m \times</math> circular acceleration formula            State correct equation <math>T\sin\alpha = m\omega^2 l\sin\alpha</math>            Eliminate <math>T</math> and obtain given answer <math>\cos\alpha = \frac{g}{\omega^2 l}</math> correctly</p> <p>OR: Equate <math>mg\sin\alpha</math> to <math>m \times</math> circular acceleration formula <math>\times \cos\alpha</math>            State correct equation <math>mg\sin\alpha = m\omega^2 l\sin\alpha\cos\alpha</math>            Obtain given answer <math>\cos\alpha = \frac{g}{\omega^2 l}</math> correctly</p> <p>(i) Use Hooke's law to express <math>T_{PQ}</math> in terms of <math>m, g, l, \theta</math>            Cancel <math>l</math> and obtain correct expression <math>mg(2\sin\theta - 1)</math> or equivalent</p> <p>(ii) State a 3-term Newton II equation <math>T_{OP}\sin\theta + T_{PQ} = mr \times \frac{2g}{l}</math> (ie <math>w^2 = \frac{2g}{l}</math> used)            Use <math>T_{OP}\cos\theta = mg</math> and eliminate both tensions            State correct equation involving <math>m, g, l, \theta</math> only (at most), e.g.  <math display="block">\frac{mg}{\cos\theta}\sin\theta + \frac{mg(l\sin\theta - \frac{1}{2}l)}{\frac{1}{2}l} = m\sin\theta \times \frac{2g}{l}</math> (FT on <math>T_{PQ}</math>)            Simplify and obtain answer <math>\theta = \frac{1}{4}\pi</math> or <math>45^\circ</math> correctly</p>	<p>B1            M1            A1            A1            M1            A2            A1            M1            A1            M1*            M1 (dep *)            A1 ft            A1</p>	<p>4            2            4</p>
13	<p>State or imply no sliding if <math>W\sin\alpha \leq \mu W\cos\alpha</math> (or =)            Obtain given answer <math>\mu \geq \frac{3}{4}</math> correctly            [For a direct quote of <math>\mu \geq \tan\alpha</math> allow B2]            Resolve parallel to the plane for 'sliding up' (allow sign and trig errors)            Obtain <math>P = W\sin\alpha + \mu W\cos\alpha</math>            Obtain given answer <math>P = \frac{1}{5}(3 + 4\mu)W</math> correctly            Take moments about bottom right for 'toppling up' (allow trig errors) (<math>R</math> and <math>F</math> must act through bottom right)            Obtain <math>Pl = \frac{1}{2}Wl\sin\alpha + \frac{1}{2}Wl\cos\alpha</math> or <math>Pl = W\left(\frac{1}{2}l\sqrt{2}\right)\cos(45^\circ - \alpha)</math> (or equiv in <math>P, W, l, \alpha</math>)            Substitute for <math>\alpha</math> (allow use of <math>\cos 8.1301\dots^\circ</math>) and obtain given answer <math>P = \frac{7}{10}W</math>            EITHER: Find the least possible value of <math>P</math> for sliding and compare with <math>\frac{7}{10}W</math>            State that as <math>\frac{7}{10}W &lt; \frac{6}{5}W</math>, toppling occurs first            OR: Find the least possible value of <math>\mu</math> for toppling to occur before sliding and compare with <math>\frac{3}{4}</math>            State that as <math>\frac{1}{8} &lt; \frac{3}{4}</math>, toppling occurs first</p>	<p>M1            A1            M1            A1            A1            M1            A1            A1            M1            A1            M1            A1            M1            A1</p>	<p>2            3            3            2</p>

14	<p>(a) (i) State any one Newton II equation, e.g. <math>0.3g - T = 0.3a</math>, <math>T - 0.2g = 0.2a</math>, <math>0.1g = 0.5a</math>            State two of the above equations correctly            Solve a relevant pair of equations to find <math>T</math>            Obtain answer <math>T = 2.4</math></p> <p>(ii) State or use <math>a = \frac{1}{5}g</math> in this part of the question            Use <math>v = u + at</math> with <math>u = 0</math> and <math>a \neq g</math> to find <math>t</math>            Obtain answer <math>t = 2.0</math></p> <p>[Answer to (i) and (ii) left as <math>6g/26</math> and <math>20/g</math> are penalised once, scoring A0 A1]            [NB: if <math>g</math> is omitted only the M marks are available.]</p> <p>(b) EITHER: State equation or inequality, with 3 force terms, for motion parallel to the plane for either particle            Resolve perpendicular to the plane for either particle, and use <math>F = \mu R</math>            State one correct equation/inequality, e.g.  <math>0.3g\sin 30^\circ - 0.3\mu g\cos 30^\circ - T = 0.3a</math> (or <math>&gt; 0</math> or <math>= 0</math>)            State a second correct equation/inequality, eg  <math>T - 0.2g\sin 30^\circ - 0.2\mu g\cos 30^\circ = 0.2a</math> (or <math>&gt; 0</math> or <math>= 0</math>)            Eliminate <math>T</math> from a pair of equations or inequalities and solve for <math>\mu</math>            Obtain the given inequality <math>\mu &lt; \frac{1}{5\sqrt{3}}</math> correctly and not via decimals</p> <p>OR:            State 'system' equation or inequality involving both weight components and both friction forces            Resolve perpendicular to the plane for both particles, and use <math>F = \mu R</math>            State any correct equation/inequality, e.g. <math>0.1g\sin 30^\circ - 0.5\mu g\cos 30^\circ = 0.5a</math> (or <math>&gt; 0</math> or <math>= 0</math>)            Solve this equation/inequality for <math>\mu</math>            Obtain given inequality <math>\mu &lt; \frac{1}{5\sqrt{3}}</math> correctly and not via decimals</p>	<p>M1 A1 M1 A1 B1 M1 A1 M1 M1 A1 M1 M1 A1 M1 M1 A2 M1 A1</p>	<p>4 3 6</p>
15	<p>(i) State driving force = <math>\frac{10000}{25}</math>            State 3-term Newton II equation <math>\frac{10000}{25} - 200 = 400a</math>            Obtain answer <math>a = \frac{1}{2}</math></p> <p>(ii) Obtain answer 20 (i.e. <math>\frac{10}{\text{answer(i)}}</math>)</p> <p>(iii) Use <math>a = \frac{dv}{dt}</math> to set up DE, and attempt separation of variables            Obtain <math>\int \frac{2v}{50-v} dv = \int dt</math>, or equally integrable equivalent            Obtain both <math>2\{-v - 50\ln(50-v)\}</math> and <math>t</math> correctly            Obtain given answer 20.5 correctly, either via limits or <math>+c</math>            [Follow through on wrong factor of 2 only]</p> <p>(iv) Set up and separate new DE: <math>\int \frac{2v^2}{50-v} ds = \int ds</math>, or equally integrable equivalent            Obtain <math>2\{-\frac{1}{2}v^2 - 50v - 50^2\ln(50-v)\}</math> and <math>s</math> correctly            Obtain answer 527            [Follow through on wrong factor of 2 only]</p> <p>(v) State equation involving WD by engine, WD against resistance, KE            State or imply work done by engine is <math>10000t</math>            State or imply work done against resistance is <math>200s</math>            Prove given answer correctly</p>	<p>B1 M1 A1 B1 ft M1 A1 A1 ft A1 M1 A1 ft A1 M1 B1 B1 A1</p>	<p>3 1 4 3 4</p>



RECOGNISING ACHIEVEMENT

UCLES

Markscheme 9200/4  
June 2000



June 2000

9200/04 A Level Linear Mathematics

1	<p>EITHER: Attempt quotient rule (or equivalent) allowing sign errors for this mark (products reversed only)</p> <p>Obtain any correct unsimplified expression, e.g. <math>\frac{(2x+1) \times 1 - (x-2) \times 2}{(2x+1)^2}</math></p> <p>Obtain simplified answer <math>\frac{5}{(2x+1)^2}</math> correctly</p> <p>[Product rule also requires chain rule (both applied correctly for M1)]</p> <p>OR: Express the function as <math>\frac{1}{2} - \frac{5}{2(2x+1)}</math></p> <p>Use chain rule to differentiate <math>k(2x+1)^{-1}</math> (result <math>-k(2x+1)^{-2}</math> is M0)</p> <p>Obtain simplified answer <math>\frac{5}{(2x+1)^2}</math> correctly</p> <p>[Accept final answer in the form <math>\frac{5}{4x^2+4x+1}</math>.]</p>	<p>M1 A1 A1 B1 M1 A1</p>	3
2	<p>EITHER: State or imply correct cosine rule (in any form) involving 2, 3, 4 and either B or C</p> <p>Obtain <math>\cos B = -\frac{1}{4}</math> (aef) or <math>B = 104.5^\circ</math> or <math>104^\circ</math> or <math>105^\circ</math> or <math>\cos C = \frac{7}{8}</math> (aef) or <math>C = 29^\circ</math></p> <p>State or imply correct formula for <math>AD^2</math> involving 2, 4 and their numerical <math>\cos B</math> or 1, 4 and their numerical <math>\cos(180 - C)</math> or <math>-\cos C</math></p> <p>Obtain answer <math>\sqrt{24}</math> or <math>2\sqrt{6}</math> or 4.9</p> <p>OR: [E is the foot of the perpendicular from A to CB produced]</p> <p>Use Pythagoras in triangles ACE and ABE to obtain an equation for BE or AE</p> <p>Obtain <math>BE = \frac{1}{2}</math> or <math>AE^2 = \frac{15}{4}</math></p> <p>Apply Pythagoras (or trig) with numerical BE and/or AE to find <math>AD^2</math> (or AD)</p> <p>Obtain answer <math>\sqrt{24}</math> or <math>2\sqrt{6}</math> or 4.9</p>	<p>M1* A1 M1 (dep *) A1 M1* A1 M1 (dep *) A1</p>	4
3	<p>(i) Multiply two relevant probabilities for a 'Yes' branch</p> <p>Add the two relevant two-factor cases, i.e. <math>\frac{2}{3}p + \frac{1}{3}(1-p)</math></p> <p>Obtain given answer <math>\frac{1}{3}(1+p)</math> correctly</p> <p>(ii) (Solve <math>\frac{1}{3}(1+p)</math> and) find <math>p = 0.05</math></p> <p>Divide attempted P('No' and 'Truthful') by P('No')</p> <p>State or imply answer is <math>\frac{\frac{2}{3}(1-0.05)}{1-0.35}</math></p> <p>Obtain answer 0.97 or <math>\frac{38}{39}</math> or equivalent fraction</p> <p>[M1 is for a fraction with numerical numerator <math>\frac{2}{3}(1-p)</math> or denominator <math>1-0.35</math> (or equivalent); ft only if <math>0 &lt; p &lt; 1</math>]</p>	<p>M1* M1 (dep *) A1 B1 M1 A1 ft A1</p>	3 1 3

4	(a) (i) State 'pie chart' or 'bar chart' or 'pictogram' or 'line diagram'	B1	1
	(ii) State 'histogram' or 'stem and leaf diagram' or 'frequency polygon' or 'cumulative frequency diagram'	B1	1
	(iii) State 'double bar chart' or 'two bar charts with common scales on a single diagram'	B1	1
(b) (i) Read off at least one relevant result Obtain any one answer 32, 38, 43 Obtain all three correct values of the median and quartiles, identifying the median State interquartile range is 11	M1		
	A1		
	A1 A1 ft		4
(ii) Show linear scale from 0 to 60 with 0 and 60 marked and with ends of whiskers located at 5 and 60 Show box extending between their quartile values Show median line in box at their median value	B1 B1 ft B1 ft		3
[Location of 5, medians and quartiles to be reasonably consistent with a linear scale.]			
5	State procedure A is better	B1	
	Indicate that early customers may not be typical of customers in general [For the justification mark, it's no good <i>merely</i> saying 'not random' or biased.] State any sensible idea, involving e.g. useful criticisms from people who don't use her shop, useful ideas for attracting new customers, etc, etc. [not enough to say 'not random' or 'to avoid bias']	B1 B1	2
6	Form an expression for $\sum x^2 p$	M1 *	
	Subtract $(\sum xp)^2$ from the above	M1 (dep *)	
	Obtain correct expression $6p - 16p^2$ for the variance	A1	
	Equate variance (not s.d.) to $\frac{1}{2}$ and solve for $p$	M1	
	Obtain values $p = \frac{1}{4}$ and $p = \frac{1}{8}$	A1	
Deduce both values 1 and $\frac{1}{2}$ for $E(X)$ The ft is only 2 $p$ values $0 < p < 1$		A1 ft	6
7	(i) State or imply one of the 2 binomial terms $\binom{50}{1} (0.88)^{49} (0.12)$		
	or $\binom{50}{2} (0.88)^{48} (0.12)^2$	M1	
	Add the correct three binomial terms (and no others)	M1	
	Obtain answer 0.051	A1	3
(ii) State or imply $\mu = 50 \times 0.12$ State or imply value $50 \times 0.12 \times 0.88$ relating to variance/s.d. Evaluate $\frac{9.5-6}{\sqrt{(5.28)}}$ and use tables Obtain answer 0.064	B1 B1		
	M1		
	A1		4
[The M1 is not lost for missing continuity correction, or for c.c. of $\frac{1}{2}$ on the wrong side, but the denominator must be $\sqrt{(npq)}$ not $npq$ .]			
SR1 Incorrect use of Poisson could score B1 for $\mu = 6$ and B1 for final answer 0.084 SR2 If $p/q$ interchanged can score M1 M1 A0 B0 B1 M1 A0 NB <sub>1</sub> use of Binomial in (ii) scores M0 NB <sub>2</sub> in (i) and (ii) treat $p = \frac{12}{50}$ as MR			
8	(i) Use correct Poisson formula with $\mu = 4$ , i.e. $e^{-4} \frac{4^3}{3!}$	M1	
	Obtain answer 0.20	A1	2
	(ii) Add correct Poisson cases 0, 1, 2 Obtain answer 0.24	M1 A1	2
State or imply Poisson with $\mu = 5$ is a suitable model OR if 2 distributions considered separately, consider <i>all</i> cases Calculate $1 - \{P(0) + P(1) + P(2) + P(3)\}$ Obtain answer 0.73 or 0.74 (0.73497...)		B1 M1 A1	3



11	<p>Show evidence of correct binomial term <math>\binom{24}{2}(0.8)^{22}(0.2)^2</math></p> <p>Add the three relevant terms for 0, 1, 2 sufferers or <math>1 - (0, 1, 2 \text{ sufferers})</math>  Obtain value 0.11 (consistent with comparison to 0.1) or obtain value 0.89 (consistent with comparison to 0.9)  Compare 0.11 to 0.1 or compare 0.89 to 0.9 and accept NH, i.e. can't reject <math>p = 0.2</math></p> <p>EITHER: State or use 0.2 and <math>\sqrt{\left(\frac{0.2 \times 0.8}{40}\right)}</math> as normal mean and s.d.</p> <p>State observed proportion is <math>\frac{12}{40} = 0.3</math></p> <p>Calculate <math>\frac{\pm(0.3-0.2)}{\sqrt{0.004}}</math> and use tables for this z value or use tables for 0.1</p> <p>Obtain tail probability 0.057 or obtain 1.58 for test statistic and 1.28(2)  Compare tail probability to 0.1 OR compare 1.58 to 1.28(2) and reject NH; i.e. accept <math>p &gt; 0.2</math>  [strictly speaking the observed proportion should be taken as <math>\frac{11.5}{40} = 0.2875</math>; the conclusion is unchanged.]</p> <p>OR: State or use <math>40 \times 0.2</math> as the mean for a normal distribution  State or use <math>\sqrt{(40 \times 0.2 \times 0.8)}</math> as the s.d.</p> <p>Calculate <math>\frac{\pm(11.5-8)}{\sqrt{6.4}}</math> and use tables for this z value or use tables for 0.1</p> <p>Obtain tail probability 0.083 or obtain 1.38 for test statistic and 1.28(2)  Compare tail probability to 0.1 or compare 1.38 to 1.28(2) and reject NH, i.e. accept <math>p &gt; 0.2</math>  [NB no cc or wrong cc can still gain M mark]</p> <p>OR: If binomial test carried out:  One correct Binomial term  Calculate <math>1 - \Sigma</math> relevant terms 0 ... 11 (allow 12 error)  Obtain value 0.087 or 0.088  Compare to 0.1 and reject NH</p>	<p>B1</p> <p>M1</p> <p>A1</p> <p>A1 ft</p> <p>B1</p> <p>B1</p> <p>M1</p> <p>A1</p> <p>A1 ft</p> <p>B1</p> <p>B1</p> <p>M1</p> <p>A1</p> <p>A1 ft</p> <p>B1</p> <p>M1</p> <p>A2</p> <p>A1 ft</p>	<p>4</p> <p>5</p>
12	<p>(i) State that the data must be a sample from a normal population</p> <p>(ii) State or use <math>\bar{x} = 27.5</math></p> <p>Show correct expression for either unbiased or biased variance estimate</p> <p>Calculate <math>\frac{\pm(27.5-36)}{\text{attempted s.e.}}</math></p> <p>Show correct value <math>\frac{27.5-36}{\sqrt{\left(\frac{36.28}{10}\right)}}</math> or <math>\frac{27.5-36}{\sqrt{\left(\frac{32.65}{9}\right)}}</math> (<math>= -4.46</math>)</p> <p>State or imply 9 degrees of freedom</p> <p>Demonstrate the given result via comparison <math>4.46 &gt; 4.297</math></p> <p>Equate <math>\frac{27.5-\mu}{\text{attempted s.e.}}</math> to numerical t-value</p> <p>State or use <math>t = -1.833</math></p> <p>Obtain answer 31</p>	<p>B1</p> <p>B1</p> <p>B1</p> <p>M1</p> <p>A1 ft</p> <p>B1</p> <p>A1</p> <p>M1</p> <p>B1</p> <p>A1</p>	<p>1</p> <p>6</p> <p>3</p>

13	<p>Show evidence of substituting relevant numbers into a correct formula Obtain answer 0.99 correctly [If done by calculator with no working, the marks are B3 or B0] make a sensible comment, e.g. consistent with a linear relationship, strong positive correlation</p> <p>use the <math>d-v</math> data correctly to find the line of <math>d</math> on <math>v</math> obtain equation <math>d = -25.5 + 1.64v</math> [If done by calculator with no working, the marks are B2 or B0] Show axes with required scaling Show the six points plotted correctly Show the calculated line correctly – check <math>v</math> intercept accuracy <math>\pm \frac{1}{2}</math> square – check <math>v = 40</math> (<math>d = 40.1</math>) accuracy <math>\pm \frac{1}{2}</math> square or similar</p> <p>Use the equation or plot of the regression line and obtain <math>d = 65</math> or <math>64</math> completely correctly</p> <p>Make any sensible comment, e.g. plot of data shows evidence of a non-linear relationship, regression line overestimates <math>d</math> when <math>v = 55</math>, value of coefficient (or data plot) suggests line will be suitable</p>	<p>M1 A1</p> <p>B1 M1 A1</p> <p>B1 B1</p> <p>B1 ft</p> <p>B1</p> <p>B1</p>	<p>3</p> <p>1 2</p> <p>3 1 1</p>
14	<p>(i) State numerical expression of the form <math>\left(\frac{3}{4}\right)^n \left(\frac{1}{4}\right)</math>, with <math>n = 3</math> or <math>4</math> Obtain answer <math>\frac{27}{256}</math> or 0.11</p> <p>(ii) EITHER: Attempt addition of relevant terms <math>\left(\frac{3}{4}\right)^n \left(\frac{1}{4}\right)</math> Obtain answer <math>\frac{21087}{65536}</math> or 0.32 OR: Attempt relevant subtraction <math>\left(\frac{3}{4}\right)^3 - \left(\frac{3}{4}\right)^8</math> Obtain answer <math>\frac{21087}{65536}</math> or 0.32</p> <p>(iii) State expression <math>\left(\frac{3}{4}\right)^n \left(\frac{1}{4}\right)^2</math> for one case Add probabilities for the two cases FSS, SFS (or equivalent) Obtain answer <math>\frac{3}{32}</math> or 0.094</p> <p>State or imply value 4 for mean <math>\mu</math> of <math>X</math> State or imply value 12 for variance <math>\sigma^2</math> of <math>X</math> Show numerical calculation <math>\frac{5-\mu}{\text{st. error}}</math> where the denominator involves their 12 and 60 Show correct expression <math>\frac{5-4}{\sqrt{\left(\frac{12}{60}\right)}}</math> Obtain answer 0.013 correctly</p>	<p>M1 A1</p> <p>M1 A1</p> <p>M1 A1</p> <p>B1 M1 A1</p> <p>B1 B1</p> <p>M1</p> <p>A1 ft</p> <p>A1</p>	<p>2</p> <p>2</p> <p>3</p> <p>5</p>
15	<p>(i) Calculate all expected frequencies Obtain all values 117.03 50.29 15.04 5.64 131.97 56.71 16.96 6.36 Carry out correct method for calculation of <math>\chi^2</math> Obtain value 3.29 for <math>\chi^2</math> State or imply 3 degrees of freedom Compare 3.29 with 7.815 and conclude there's no association [If 6 or 7 of the expected frequencies are correct, allow A1. For accuracy only to 2 s.f. or nearest whole number allow A1 for all correct to this accuracy]</p> <p>(ii) State or use <math>\frac{207}{400} = 0.5175</math> or 0.52 for Poisson mean Use <math>Po(0.5175)</math> to calculate four expected frequencies Obtain values 238.40, 123.36 or 123.37, 31.92, 6.30 to 6.32 (for 3 or more) Carry out correct method for calculation of <math>\chi^2</math> Obtain value 7.75 to 7.80 State or imply 2 degrees of freedom Compare 7.80 with 5.99 and conclude it doesn't fit [Special case: candidates whose fourth frequency is 5.51 (for 3) and who incorrectly use this instead of the frequency for 3 or more can score B1 M1 A0 M1 A0 B1 and A1 ft for comparing their <math>\chi^2 \approx 10.29</math> with 5.99]</p>	<p>M1 A2</p> <p>M1 A1 B1 ft A1 ft</p> <p>B1 M1 A1 M1 A1 B1 ft A1 ft</p>	<p>7</p> <p>7</p>